# Ab Initio/IGLO/GIAO-MP2 Study of Hypercoordinate Square-Pyramidal Carbocations ${ }^{1}$ 

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#### Abstract

The structures of hypercoordinate square-pyramidal carbocations were calculated at the correlated MP2/6$31 G^{*}$ level. The ${ }^{13} \mathrm{C}$ NMR chemical shifts of the cations were also calculated using IGLO and GIAO-MP2 methods. The IGLO calculated data show only a reasonable correlation with the experimental ${ }^{13} \mathrm{C}$ NMR chemical shifts. The correlated GIAO-MP2 calculated ${ }^{13} \mathrm{C}$ NMR shifts, however, showed significant improvements over the SCF IGLO calculated chemical shifts. It was also found that among the $\mathrm{C}_{8} \mathrm{H}_{9}{ }^{+}$isomers, the bishomo square-pyramidal cation 7 is only $0.2 \mathrm{kcal} / \mathrm{mol}$ more stable than the trishomocyclopropeniumtype ion $\mathbf{8}$ at the MP4(SDQ)/6-31G*//MP2/6-31G $*+$ ZPE level. Almost a calculated $1: 2$ equilibrium mixture of ions $\mathbf{7}$ and $\mathbf{8}$ seems to best represent the experimental NMR spectrum of $\mathrm{C}_{8} \mathrm{H}_{9}{ }^{+}$at $-80{ }^{\circ} \mathrm{C}$. The structures and ${ }^{13} \mathrm{C}$ NMR chemical shifts for the elusive $(\mathrm{CH})_{5}{ }^{+} \mathbf{1}$ and its monomethyl-substituted analogues $\mathbf{2}$ and $\mathbf{3}$ were also computed.


## Introduction

Hypercoordinate square-pyramidal carbocations have been the focus of much interest and speculation over the past two decades. ${ }^{2,3}$ In 1971, Williams ${ }^{4}$ first suggested the hypercoordinate square-pyramidal structure for the $(\mathrm{CH})_{5}{ }^{+}$carbocation based on the structure of isoelectronic isostructural pentaborane. In 1972, Stohrer and Hoffmann ${ }^{5}$ concluded from a theoretical treatment using extended Hückel formalism that the energy minimum for the $(\mathrm{CH})_{5}{ }^{+}$cation does not correspond to a planar classical structure. The proposed structure was three-dimensional in the form of a square pyramid with multicenter bonding.

$(\mathrm{CH}) 5^{+}$


In the same year Masamune and co-workers ${ }^{6}$ presented experimental evidence for a dimethyl analogue $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{C}_{5} \mathrm{H}_{3}{ }^{+}$ in superacid solution and concluded that the structure is indeed a square pyramid, and thus, a structural and isoelectronic relationship with 1,2-( $\left.\mathrm{CH}_{3}\right)_{2} \mathrm{~B}_{5} \mathrm{H}_{7}$ was established.



Although the parent cation $(\mathrm{CH})_{5}{ }^{+}$has not yet been observed experimentally, a variety of similar structures ${ }^{6-10}$ have been identified under stable ion conditions using ${ }^{13} \mathrm{C}$ and ${ }^{1} \mathrm{H}$ NMR
spectroscopy. The pentagonal-pyramidal structure was observed for the $\left(\mathrm{CCH}_{3}\right)_{6}{ }^{2+}$ dication: ${ }^{11}$


The $(\mathrm{CH})_{5}{ }^{+}$cation has also been a subject of many theoretical studies first by semiempirical and later by ab initio methods. Kollman et al. ${ }^{12}$ and Dewar and co-workers reported ${ }^{13}$ CNDO and MINDO/3 studies on $(\mathrm{CH}) 5^{+}$, respectively. Ab initio calculation on capped annulene rings with six interstitial electrons was carried out by Schleyer et al. ${ }^{14,15}$ Results of this calculation show that the favorable pyramidal structure follows the Hückel-like $4 n+2$ interstitial electron rule.

We now wish to report our ab initio/IGLO/GIAO-MP2 studies of a series of square-pyramidal carbocations, which were characterized earlier by ${ }^{1} \mathrm{H}$ and ${ }^{13} \mathrm{C}$ NMR spectroscopy under long-lived stable ion conditions. This permits comparison of calculated data with the experimentally observed results. We have also calculated the structures and ${ }^{13} \mathrm{C}$ NMR chemical shifts for the still elusive $(\mathrm{CH})_{5}{ }^{+}$carbocation and its monomethyl analogues.

## Results and Discussions

Ab initio calculations were carried out by using the Gaussian $94^{16}$ package of programs. Geometries were optimized at the HF/6-31G* and MP2/6-31G* levels. Vibrational frequencies at the HF/6-31G*//HF/6-31G* level were used to characterize stationary points as minima and to evaluate zero-point vibrational energies (ZPE). For some of the cations single-point energies at the MP4(SDQ)/6-31G* level on MP2/6-31G*


Figure 1. MP2/6-31G* optimized structures of $\mathbf{1 - 1 0}$.
geometries were calculated. Selected parameters of the ions at the MP2/6-31G* level are given in Figure 1. IGLO calculations were performed according to a reported method ${ }^{17-19}$ at IGLO DZ and II levels using MP2/6-31G* geometries. Huzinaga ${ }^{20 a}$ Gaussian lobes were used as follows. Basis DZ: C, 7s3p contracted to [4111, 21]; H, 3s contracted to [21]. Basis II: C, 9 s 5 p 1 d contracted to [51111, 2111, 1]; d exponent, 1.0; H, 5s1p contracted to [311, 1]; p exponent, 0.70 . GIAO-MP2 calculations using $3-21 \mathrm{G},{ }^{20 \mathrm{~b}} \mathrm{dzp} / \mathrm{dz},{ }^{21,22}$ and tzp/dz basis sets ${ }^{21,22}$ on MP2/6-31G* geometries have been performed with the ACES II program. ${ }^{23}$ Relevent computed and reported chemical shifts are listed in Table 1.

Square-Pyramidal Carbocations. $(\mathrm{CH})_{5}{ }^{+} 1, \mathrm{CH}_{3} \mathrm{C}_{5} \mathrm{H}_{4}^{+}$2, $\mathrm{CH}_{3} \mathrm{C}_{5} \mathrm{H}_{4}^{+}$3, $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{C}_{5} \mathrm{H}_{3}{ }^{+}$4, and $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{C}_{5} \mathrm{H}_{2}{ }^{+}$5. The parent square-pyramidal ion $\mathbf{1}$ has not yet been observed. The MP2/

TABLE 1: Calculated and Experimental ${ }^{13}$ C NMR Chemical Shifts ${ }^{a}$

| no. | position | atom | IGLO |  | GIAO-MP2 |  |  | exptl |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | DZ ${ }^{b}$ | II ${ }^{\text {b }}$ | 3-21G | dzp/dz | tzp/dz ${ }^{\text {b }}$ |  |
| 1 | apical | C1 | -36.2 | -52.0 | -34.1 | -35.3 | -37.4 |  |
|  | basal | C2 | 78.4 | 62.7 | 65.9 | 68.3 | 71.5 |  |
| 2 | apical | C1 | -36.7 | -44.9 | -28.9 | -26.3 |  |  |
|  | basal | C2 | 76.7 | 63.4 | 66.7 | 70.0 |  |  |
|  |  | C3 | 80.3 | 66.9 | 69.2 | 72.9 |  |  |
|  |  | C4 | 83.9 | 70.5 | 71.7 | 75.8 |  |  |
|  | other | C6 | 3.6 | -0.8 | 5.4 | 3.4 |  |  |
| 3 | apical | C1 | -33.6 | -47.7 | -29.8 | -30.4 |  |  |
|  | basal | C2 | 93.4 | 83.4 | 83.2 | 89.8 |  |  |
|  |  | C3 | 77.8 | 62.8 | 66.5 | 68.6 |  |  |
|  |  | C4 | 70.2 | 53.8 | 58.1 | 59.7 |  |  |
|  | other | C6 | 10.0 | 5.6 | 12.3 | 10.2 |  |  |
| 4 | apical | C1 | -34.6 | -41.2 | -25.4 |  |  | -23.0 |
|  | basal | C2 | 90.4 | 81.6 | 82.2 |  |  | 93.7 |
|  |  | C3 | 79.4 | 66.5 | 69.4 |  |  | 73.0 |
|  |  | C4 | 75.0 | 61.5 | 64.0 |  |  | 61.0 |
|  | other | C6 | 9.5 | 5.3 | 12.0 |  |  | 7.5 |
|  |  | C7 | 2.8 | -2.2 | 4.4 |  |  | -1.0 |
| 5 | apical | C1 | -33.3 | -38.6 | $-21.9$ |  |  | -20.9 |
|  | basal | C2 | 84.0 | 75.2 | 76.1 |  |  | 78.5 |
|  |  | C3 ${ }^{\text {b }}$ | 79.3 | 67.0 | 70.3 |  |  | 72.6 |
|  | other | C6 | 8.5 | 4.2 | 11.5 |  |  | 5.4 |
|  |  | C8 | 1.6 | -3.4 | 3.2 |  |  | -3.2 |
| 6 | apical | C1 | -36.2 | $-36.9$ | $-15.1$ | -17.3 | -17.0 | -17.2 |
|  | basal | C2 | 43.0 | 35.9 | 37.9 | 40.3 | 41.9 | 39.4 |
|  | other | C3 | 6.5 | 4.8 | 12.7 | 9.8 | 5.0 | 8.1 |
| 7 | apical | C1 | -41.1 | -48.1 | -23.7 | -28.9 |  | 2.4 |
|  | basal | C2 | 48.1 | 36.2 | 38.9 | 40.3 |  | 30.4 |
|  | other | C3 | 24.9 | 20.3 | 30.5 | 29.4 |  | 29.0 |
|  |  | C8 | 40.8 | 38.1 | 44.4 | 47.1 |  | 41.7 |
| 8 |  | C1 | 18.2 | 0.2 | 14.1 |  |  |  |
|  |  | C2 | 20.4 | 7.9 | 16.4 |  |  |  |
|  |  | C3 | 16.6 | 10.5 | 18.7 |  |  |  |
|  |  | C5 | 32.5 | 24.7 | 32.9 |  |  |  |
|  |  | C6 | 36.2 | 31.4 | 39.6 |  |  |  |
|  |  | C8 | 36.3 | 33.8 | 40.7 |  |  |  |
| 9 | apical | C1 | -43.2 | -47.8 | -24.0 | -28.6 |  | -27.9 |
|  | basal | C2 | 42.4 | 34.6 | 36.6 | 38.8 |  | 37.7 |
|  | other | C3 | 8.0 | 10.0 | 17.5 | 16.9 |  | 14.9 |
|  |  | C8 | 9.5 | 11.6 | 16.4 | 17.0 |  | 14.2 |
| 10 | apical | C1 | -49.1 | -54.2 | -29.3 | -35.6 |  | -33.6 |
|  | basal | C2 | 42.3 | 34.6 | 36.0 | 38.3 |  | 35.3 |
|  | other | C3 | 13.4 | 11.8 | 21.2 | 20.6 |  | 17.5 |
|  |  | C8 | 141.3 | 139.7 | 112.6 | 124.7 |  | 129.9 |

${ }^{a}$ Calculated ${ }^{13} \mathrm{C}$ NMR chemical shifts were performed on MP2/6$31 \mathrm{G}^{*}$ optimized geometries and referenced to TMS (absolute shift, i.e., $\sigma(\mathrm{C})=222.6$ (IGLO DZ), 197.4 (IGLO II), 218.7 (GIAO-MP2/3-21G), 205.7 (GIAO-MP2/dzp/dz), 198.8 (GIAO-MP2/tzp/dz)). For numbering scheme, see Figure 1. ${ }^{b}$ Average calculated values of C 3 and C 5 .
$6-31 \mathrm{G}^{*}$ optimized structure of $\mathbf{1}$ is shown in Figure 1. The calculated apical carbon-basal carbon bond length of $1.566 \AA$ is $0.1 \AA$ longer than basal carbon-basal carbon bond length (1.465 Å).


Earlier calculations of the ion $\mathbf{1}$ at the $\mathrm{HF} / 3-21 \mathrm{G}$ level showed the corresponding bond lengths to be 1.589 and $1.477 \AA$, respectively. ${ }^{15}$ In structure $\mathbf{1}$ the apical carbon is bonded to the four carbon atoms and a hydrogen atom by sharing only eight valence electrons. Thus, the electron-deficient apical carbon-basal carbon bonds are as anticipated longer than basal carbon-basal carbon bonds. The IGLO DZ calculated ${ }^{13} \mathrm{C}$ NMR chemical shifts of the apical and basal carbons of $\mathbf{1}$ are

## SCHEME 1


$\boldsymbol{\delta}^{13} \mathrm{C}-36.2$ and 78.4 , respectively. The IGLO calculations using a larger basis set (i.e., basis II) gave chemical shifts of $\boldsymbol{\delta}^{13} \mathrm{C}-52.0$ and 62.7 significantly different from the corresponding IGLO DZ values. It is known ${ }^{24}$ that IGLO provides relatively poor data in calculations of ${ }^{13} \mathrm{C}$ NMR chemical shift of tertiary carbons. Thus, correlated calculations using the GIAO-MP2 method showed significant effect on the ${ }^{13} \mathrm{C}$ NMR chemical shifts of $\mathbf{1}$. GIAO-MP2 calculations using the 3-21G basis set (i.e., GIAO-MP2/3-21G) gave corresponding values of $\boldsymbol{\delta}^{13} \mathrm{C}$ of -34.1 and 65.9. However, GIAO-MP2 calculations using a larger dzp/dz basis set (i.e., GIAO-MP2/dzp/dz; dzp basis set for carbons and dz basis set for hydrogens) gave $\boldsymbol{\delta}^{13} \mathrm{C}$ of -35.3 and 68.3 only slightly different from those of GIAO-MP2/3-21G values. By use of an even larger tzp/dz basis set (i.e., GIAO-MP2/tzp/dz; tzp basis set for carbons and dz basis set for hydrogens), the calculated $\boldsymbol{\delta}^{13} \mathrm{C}$ of -37.4 and 71.5 are also very close to those of the corresponding GIAO-MP2/321 G and GIAO-MP2/dzp/dz results.

The monomethyl-substituted analogues of $\mathbf{1}$, that is, C1 (apical) substituted 2 and C2 (basal) substituted 3, have also not been observed. The structures of the cations were fully optimized at the MP2/6-31G* level (Figure 1). The cation 2 was found to be only $1.7 \mathrm{kcal} / \mathrm{mol}$ less stable than 3 at the MP4-(SDQ)/6-31G*//MP2/6-31G* level. The ${ }^{13} \mathrm{C}$ NMR chemical shifts of $\mathbf{2}$ and $\mathbf{3}$ were calculated and are compiled in Table 1.

The 1,2 -dimethyl-substituted analogue of $\mathbf{1}$, that is, $\mathbf{4}$, was observed ${ }^{6}$ as a long-lived ion and characterized by ${ }^{13} \mathrm{C}$ NMR spectroscopy. The 2,4 -dimethyl-substituted analogue of $\mathbf{1}$ was not observed experimentally. The MP2/6-31G* optimized geometry of $\mathbf{4}$ is similar to that of $\mathbf{1}$. The GIAO-MP2/3-21G calculated $\delta^{13} \mathrm{C}$ of the apical carbon of 4 is -25.4 , which is very close to the experimental value of $\delta^{13} \mathrm{C}-23.0$. However, GIAO-MP2/3-21G calculated $\delta^{13} \mathrm{C}$ of the basal carbons (82.2, 69.4, and 64.0) slightly deviate from the experimental data (93.7, 73.0, and 61.0). GIAO-MP2 calculations using larger basis sets, however, were not possible. This is because calculations using the ACES II program ${ }^{23}$ are presently limited to only to smallersized molecules (limits strongly dependent on molecular symmetry).

Trimethyl analogue 5 was also characterized ${ }^{7}$ in superacid solutions by ${ }^{13} \mathrm{C}$ NMR spectroscopy. The MP2/6-31G* optimized geometry of $\mathbf{5}$ is expectedly similar to that of $\mathbf{4}$. As in 4, the GIAO-MP2/3-21G calculated $\delta^{13} \mathrm{C}$ of the apical carbon of $\mathbf{5}$ is -21.9 , which is very close to the experimental value of $\delta{ }^{13} \mathrm{C}-20.9$. GIAO-MP2/3-21G calculated $\delta^{13} \mathrm{C}$ of the basal carbons of 5 (76.1 and 70.3) also corresponds very closely to the observed experimental values ( 78.5 and 72.6).

Bishomo Square-Pyramidal Cations. $\mathrm{C}_{7} \mathrm{H}_{9}{ }^{+}$6. The bishomo square-pyramidal ion 6 was originally prepared by Masamune et al. ${ }^{8}$ in superacid $\mathrm{SbF}_{5}-\mathrm{SO}_{2} \mathrm{ClF}$ solution at -110 ${ }^{\circ} \mathrm{C}$. The MP2/6-31G* optimized structure of $\mathbf{6}$ is given in Figure 1. We also searched for minimum-energy trishomocyclopro-penium-type structure (Scheme 1). At the MP2/6-31G* level the structure is not a minimum on the potential-energy surface of $\mathrm{C}_{7} \mathrm{H}_{9}{ }^{+}$and converged into structure $\mathbf{6}$ upon optimization. The parent persistent trishomocyclopropenium ion was also prepared by Masamune et al. ${ }^{26}$ in superacid solutions and characterized

## SCHEME 2


by ${ }^{13} \mathrm{C}$ NMR spectroscopy. The trishomocyclopropenium ion was also studied by an ab initio/IGLO method by Prakash et al., ${ }^{26}$ and its highly symmetrical $C_{3 v}$ structure was confirmed.

The ${ }^{13} \mathrm{C}$ NMR chemical shifts of 6 were calculated by the both IGLO and GIAO-MP2 methods. The IGLO II calculated $\delta^{13} \mathrm{C}$ of the apical carbon of -36.9 deviates substantially from the experimental value by -17.2 ppm . However, GIAO-MP2/ $\mathrm{dzp} / \mathrm{dz}$ calculated $\delta^{13} \mathrm{C}$ of the apical carbon of -17.3 is almost the same as the experimental value of -17.2 . These comparisons clearly demonstrate the importance of electron correlations in the calculations of the ${ }^{13} \mathrm{C}$ chemical shift of the squarepyramidal carbocations. The GIAO-MP2/dzp/dz calculated $\delta^{13} \mathrm{C}$ of the basal carbon of 40.3 ppm is also found to be very close to the experimental value of 39.4 ppm . With the larger tzp/dz basis set the GIAO-MP2 calculated $\delta^{13} \mathrm{C}$ of the apical and basal carbons of 6 are -17.0 and 41.9 , respectively, which are only slightly different from those of GIAO-MP2/dzp/dz values.
$\mathrm{C}_{8} \mathrm{H}_{9}{ }^{+}, 7$ and 8 . The $\mathrm{C}_{8} \mathrm{H}_{9}{ }^{+}$ion was prepared by Masamune et al. ${ }^{9}$ in superacid solution. Jefford and co-workers ${ }^{27}$ calculated the ion at the MINDO/3 level. Unlike $\mathrm{C}_{7} \mathrm{H}_{9}{ }^{+}$, both the bishomo square-pyramidal 7 and the trishomocyclopropenium-type structure $\mathbf{8}$ were found to be minimum-energy structures on the potential-energy surface of $\mathrm{C}_{8} \mathrm{H}_{9}{ }^{+}$at the $\mathrm{HF} / / 6-31 \mathrm{G}^{*}$ level as confirmed by the frequency calculations at the same level. The structures were further optimized at the MP2/6-31G* level. At the MP2/6-31G*//MP2/6-31G* level 7 is only $0.7 \mathrm{kcal} / \mathrm{mol}$ less stable than 8. This difference is reduced to $0.1 \mathrm{kcal} / \mathrm{mol}$ at the higher MP4(SDQ)/6-31G*//MP2/6-31G* level. By inclusion of zero-point vibrational energies (ZPE), that is, at the MP4-(SDQ)/6-31G*//MP2/6-31G* + ZPE (at the HF/6-31G*//HF/ $6-31 \mathrm{G}^{*}$ level scaled by a factor of 0.89 ), 7 is only $0.2 \mathrm{kcal} / \mathrm{mol}$ more stable than $\mathbf{8}$. Thus, structures $\mathbf{7}$ and $\mathbf{8}$ are almost isoenergetic.

The ${ }^{13} \mathrm{C}$ NMR chemical shifts of 7 were calculated by the both IGLO and GIAO-MP2 methods. The IGLO II calculated $\delta^{13} \mathrm{C}$ of the apical carbon of -48.1 largely deviates from the experimental value by 2.4 ppm . The GIAO-MP $2 / \mathrm{dzp} / \mathrm{dz}$ calculated $\delta^{13} \mathrm{C}$ of the apical carbon of -28.9 also deviates from the experimental value by 31.3 ppm .

The ${ }^{13} \mathrm{C}$ NMR chemical shifts of $\mathbf{8}$ were calculated at the GIAO-MP2/3-21G level. The calculated $\delta^{13} \mathrm{C}$ values of $\mathbf{8}$ are given in Table 1. From calculated chemical shifts of $\mathbf{7}$ and $\mathbf{8}$ it seems that the ion 7 might not be the only species involved in superacid solutions. An equilibrium mixture (undergoing rapid exchange on the NMR time scale) (Scheme 2) involving ions 7 and $\mathbf{8}$ (in 1:2 ratio) can best represent the structure of $\mathrm{C}_{8} \mathrm{H}_{9}{ }^{+}$. The calculated average chemical shifts (at the GIAO-MP2/3-21G level) of the equilibrating structures of Scheme 2 are depicted in Scheme 3 along with the experimental data obtained at $-80^{\circ} \mathrm{C}$ (in parentheses). Thus, the calculated $\delta^{13} \mathrm{C}$ of $\mathrm{C} 1-\mathrm{C} 4$ are $1.5,29.4,29.6$, and 41.9 , respectively, and match very well with the corresponding experimental values of 2.4 , $30.4,29.0$, and 41.7. The possibility of structures $\mathbf{7}$ and $\mathbf{8}$ in rapid equilibrium is not only indicated from their average chemical shifts but also from their nearly identical energies. In


Figure 2. Plot of calculated vs experimental ${ }^{13} \mathrm{C}$ NMR chemical shifts of hypercoordinate carbocations 4-6, 9, and 10: (a) IGLO DZ vs experimental results; (b) IGLO II vs experimental results; (c) GIAO-MP2/3-21G vs experimental results; (d) GIAO-MP2/dzp/dz vs experimental results.

## SCHEME 3


fact, such an equilibrium was also suggested by Masamune et al. ${ }^{9} \mathrm{C}_{8} \mathrm{H}_{9}{ }^{+}$also showed ${ }^{28}$ chemical behavior different from that of other related ions.

The relative instability of the ions 7 can also be justified from the molecular-orbital picture. The overlap between the p orbitals of the cap and the p orbitals of the 1,4 cyclohexadiene ring decreases with the bending of the $p$ orbitals away from the cap. Therefore, the good overlap between cap p orbital and 1,4 cyclohexadiene p orbitals in ion 6 is possible because of the right geometry. However, in ion 7, since the 3,6-positions of the cyclohexadiene moiety is tied (constrained) to a methylene group, the corresponding p orbitals cannot easily bend toward

## SCHEME 4


good overlap

poor overlap
the cap to make a good overlap (Scheme 4; only part of the structures are shown for simplicity).
$\mathrm{C}_{9} \mathrm{H}_{11}+9$ and $\mathrm{C}_{9} \mathrm{H}_{9}{ }^{+}$10. Both ions 9 and $\mathbf{1 0}$ were prepared by Coates et al. ${ }^{10}$ in superacid $\mathrm{SbF}_{5}-\mathrm{SO}_{2} \mathrm{ClF}$ solutions between -100 and $-130{ }^{\circ} \mathrm{C}$. The MP2/6-31G* optimized $C_{2 v}$ symmetrical structures of $\mathbf{9}$ and $\mathbf{1 0}$ are anticipated to be similar in nature (see Figure 1). Unlike in 7, in ions 9 and 10 the 3,6positions of the cyclohexadiene moiety are tied to two methylene and two methyne groups, respectively. Thus, p orbitals of the cyclohexadiene moieties of $\mathbf{9}$ and $\mathbf{1 0}$ can bend toward the cap, thus stabilizing the cationic center. However, no minimumenergy trishomocyclopropenium-type structures (Scheme 5) for $\mathrm{C}_{9} \mathrm{H}_{11}{ }^{+}$or $\mathrm{C}_{9} \mathrm{H}_{9}{ }^{+}$could be located. At the MP2/6-31G* level

## SCHEME 5


trishomocyclopropenium structure of $\mathrm{C}_{9} \mathrm{H}_{11}{ }^{+}$

trishomocyclopropenium structure of $\mathrm{CgH}_{9}{ }^{+}$
the structures are not minima on the potential-energy surfaces and converged into corresponding pyramidal (i.e., 9 and 10) structures upon optimization.

The GIAO-MP2/dzp/dz calculated $\delta^{13} \mathrm{C}$ values of the apical carbons of $\mathbf{9}$ and $\mathbf{1 0}$ are -28.6 and -35.6 , respectively. These values compare very well with the corresponding experimental results of $\delta^{13} \mathrm{C}-27.9$ and -33.6 , respectively. Similarly, the GIAO-MP2 $/ \mathrm{dzp} / \mathrm{dz}$ calculated $\delta^{13} \mathrm{C}$ of both basal carbons of 9 and $\mathbf{1 0}$ are 38.8 and 38.3 , respectively, which also compare very well with the experimental data of 37.7 and 35.3 ppm , respectively.

Chemical-Shift Correlation. Both IGLO and GIAO-MP2 calculated ${ }^{13} \mathrm{C}$ NMR chemical shifts of the hypercoordinate carbocations correlate very well with the experimental data (Figure 2). However, only the GIAO-MP2 calculated individual ${ }^{13} \mathrm{C}$ NMR chemical shifts are in excellent agreement with experimental results (Table 1) and are clearly superior to the IGLO calculated ${ }^{13} \mathrm{C}$ NMR chemical shifts.

## Conclusions

We have calculated the structures and ${ }^{13} \mathrm{C}$ NMR chemical shifts of a series of hypercoordinate square-pyramidal carbocations that were earlier characterized by ${ }^{13} \mathrm{C}$ NMR spectroscopy under long-lived stable ion conditions by ab initio calculations. IGLO calculations with either the DZ or II basis set were found to be only reasonable in reproducing the ${ }^{13} \mathrm{C}$ NMR chemical shifts of these ions. However, calculations of ${ }^{13} \mathrm{C}$ NMR chemical shifts of these ions with the correlated GIAO-MP2 method showed significant improvements over the chemicalshift results computed at the SCF level (IGLO methods). The calculations suggest that 7 is nearly identical in energy with isomeric ion 8. An almost 1:2 equilibrium mixture of ions 7 and $\mathbf{8}$ seems to best represent the observed NMR data of $\mathrm{C}_{8} \mathrm{H}_{9}{ }^{+}$ at $-80^{\circ} \mathrm{C}$. The structures and ${ }^{13} \mathrm{C}$ NMR chemical shifts for the elusive $(\mathrm{CH})_{5}{ }^{+}$ion $\mathbf{1}$ and its monomethyl-substituted analogues $\mathbf{2}$ and $\mathbf{3}$ were also computed.

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Supporting Information Available: Listing of Cartesian coordinates of the MP2/6-31G* optimized geometries and
energies at the MP2/6-31G*//MP2/6-31G* level for $\mathbf{1 - 1 0}$ (4 pages). Ordering information is given on any current masthead page.

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